

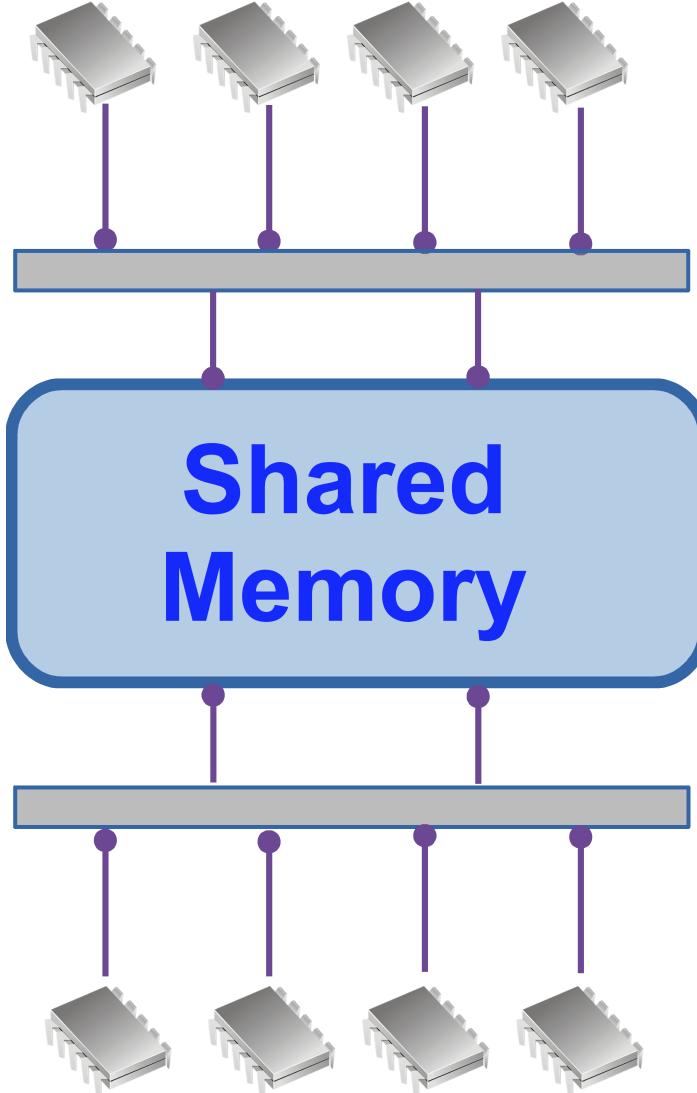
CDSSPEC: Checking Concurrent Data Structures Under the C/C++11 Memory Model

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University of California, Irvine

Feb 6, 2017

Programming Multi-core Systems



Building Blocks

**Concurrent
Data
Structures**

Concurrent Data Structures with Atomics

Implemented with
atomics

Scalability!!

Building Blocks

**Concurrent
Data
Structures**

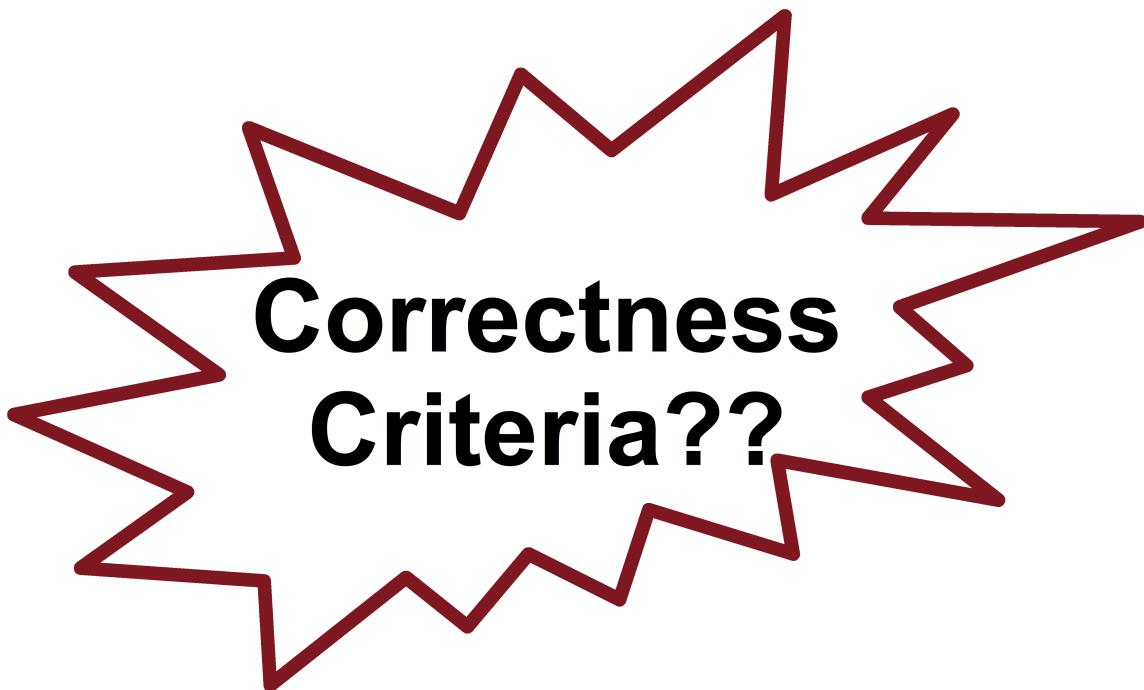
Concurrent Data Structure Correctness

Implemented with
atomics

Building Blocks

Concurrent
Data
Structures

Correctness
Criteria??



Concurrent Data Structure Correctness

Implemented with
atomics

Building Blocks

Concurrent
Data
Structures

Linearizability

Linearizability Example

```
SomeQueue x, y; // Initially empty
```

```
// Thread 1
```

```
x.enq(1);
```

```
r1=y.deq(); // → 2
```

```
// Thread 2
```

```
y.enq(2);
```

```
r2=x.deq(); // → -1
```

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```
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```

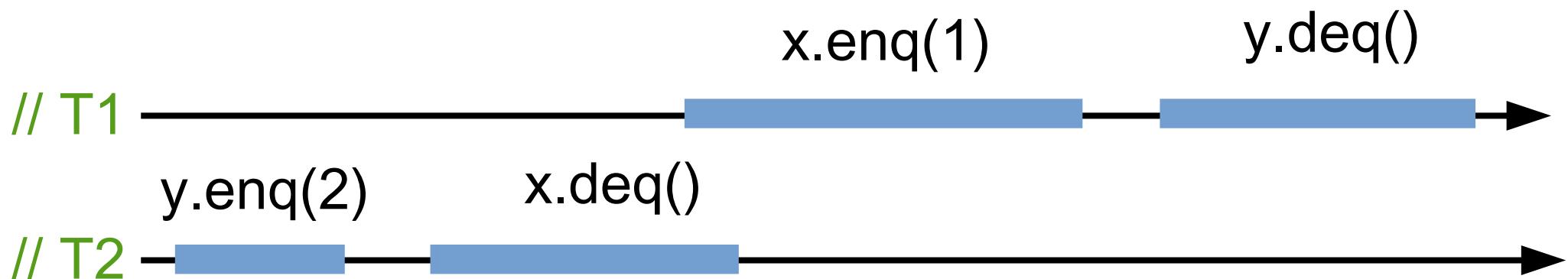
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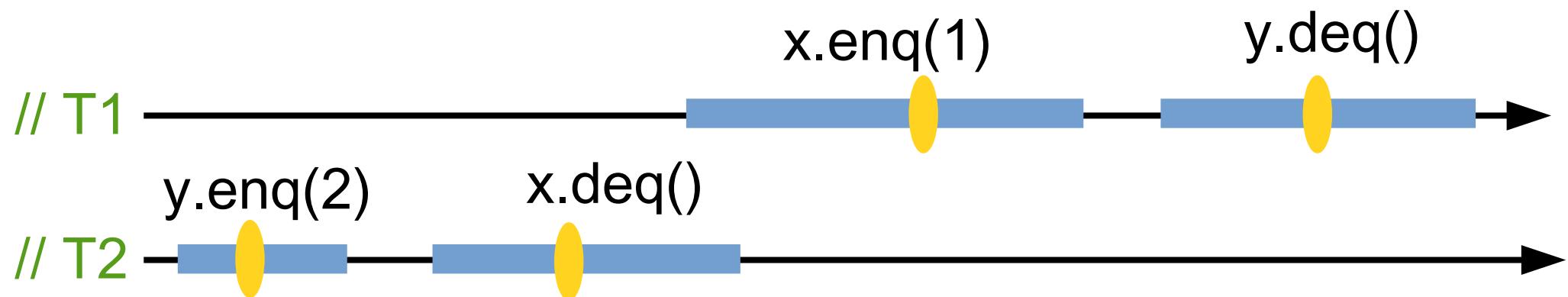
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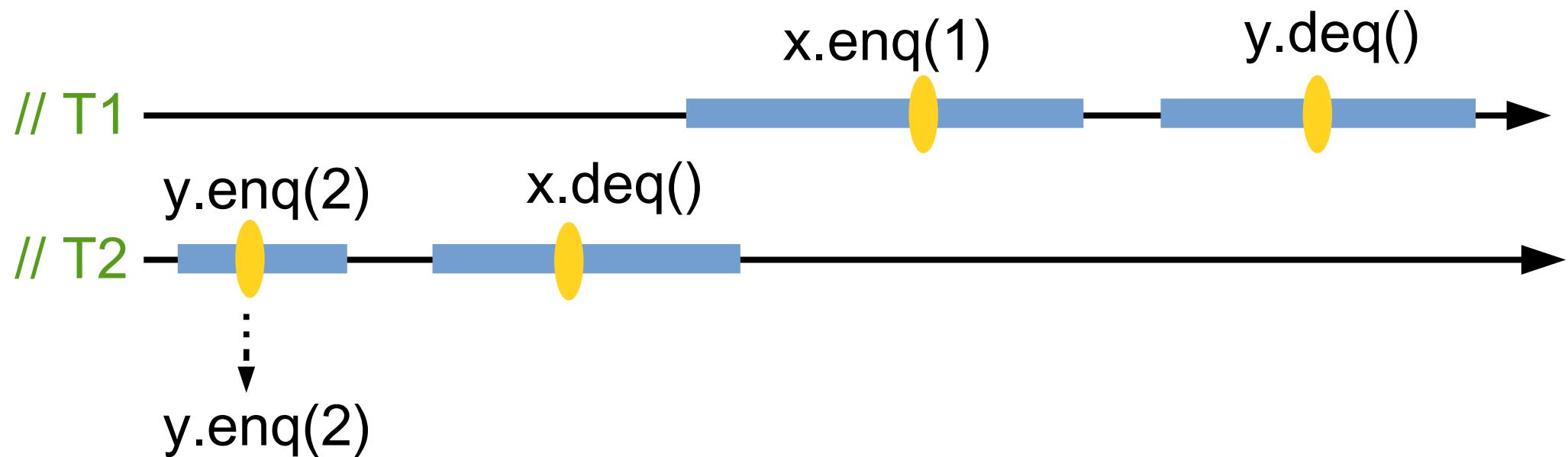
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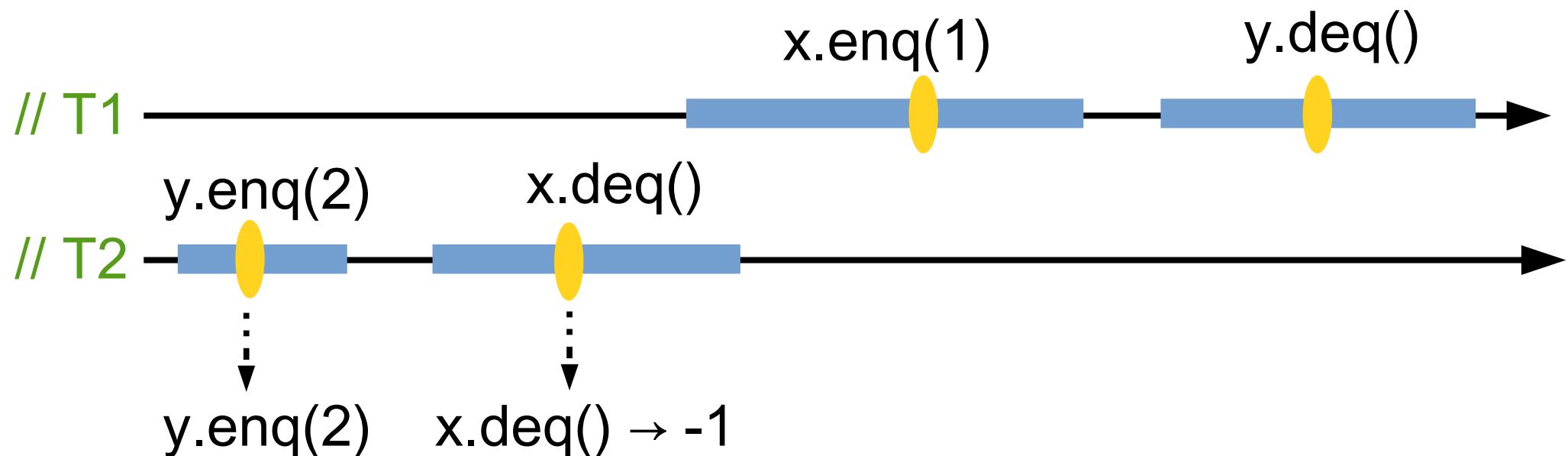
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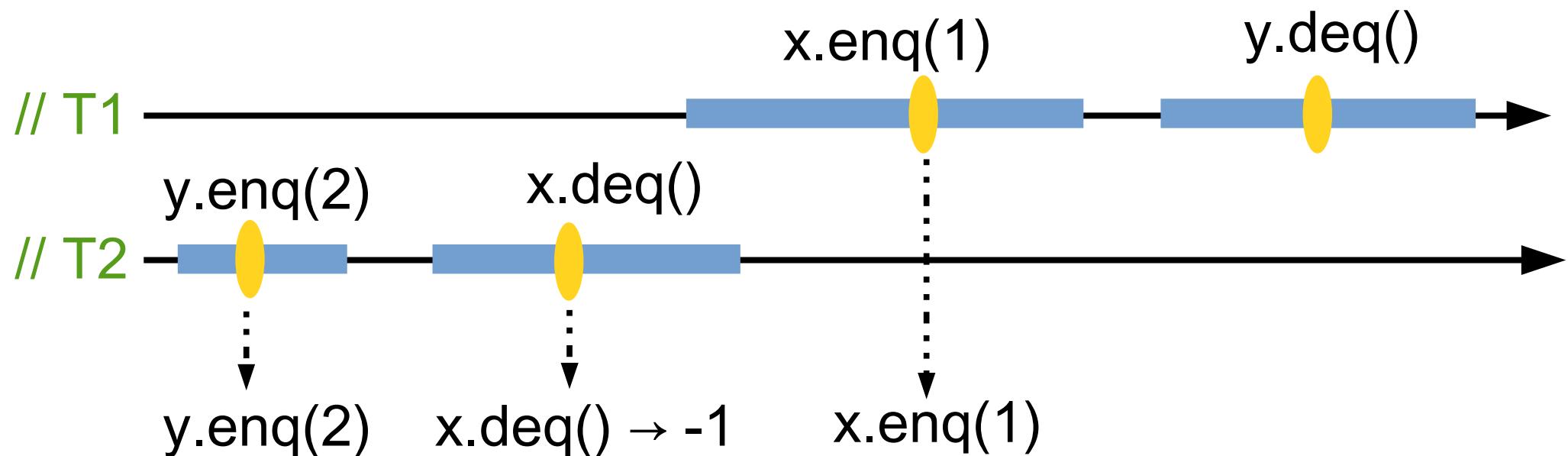
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```
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```

```
y.enq(2);
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Linearizability Example

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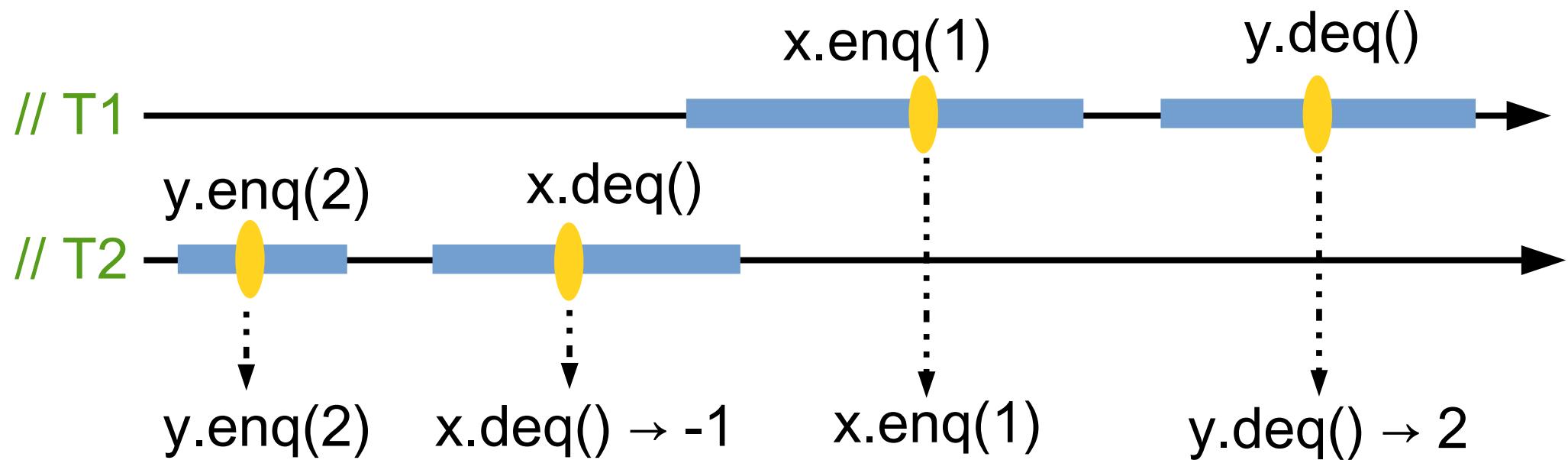
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```
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```

```
// Thread 2
```

```
y.enq(2);
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Linearizability Example

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```
// Thread 1
```

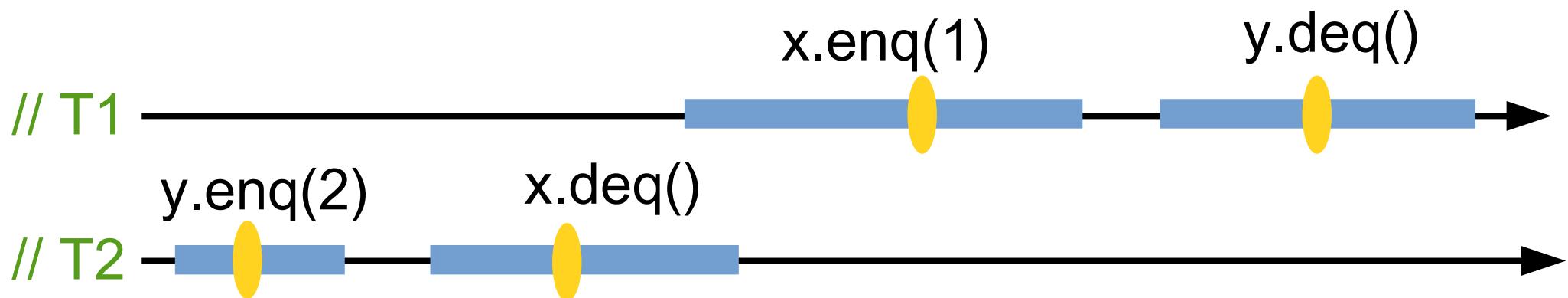
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```

```
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```

```
// Thread 2
```

```
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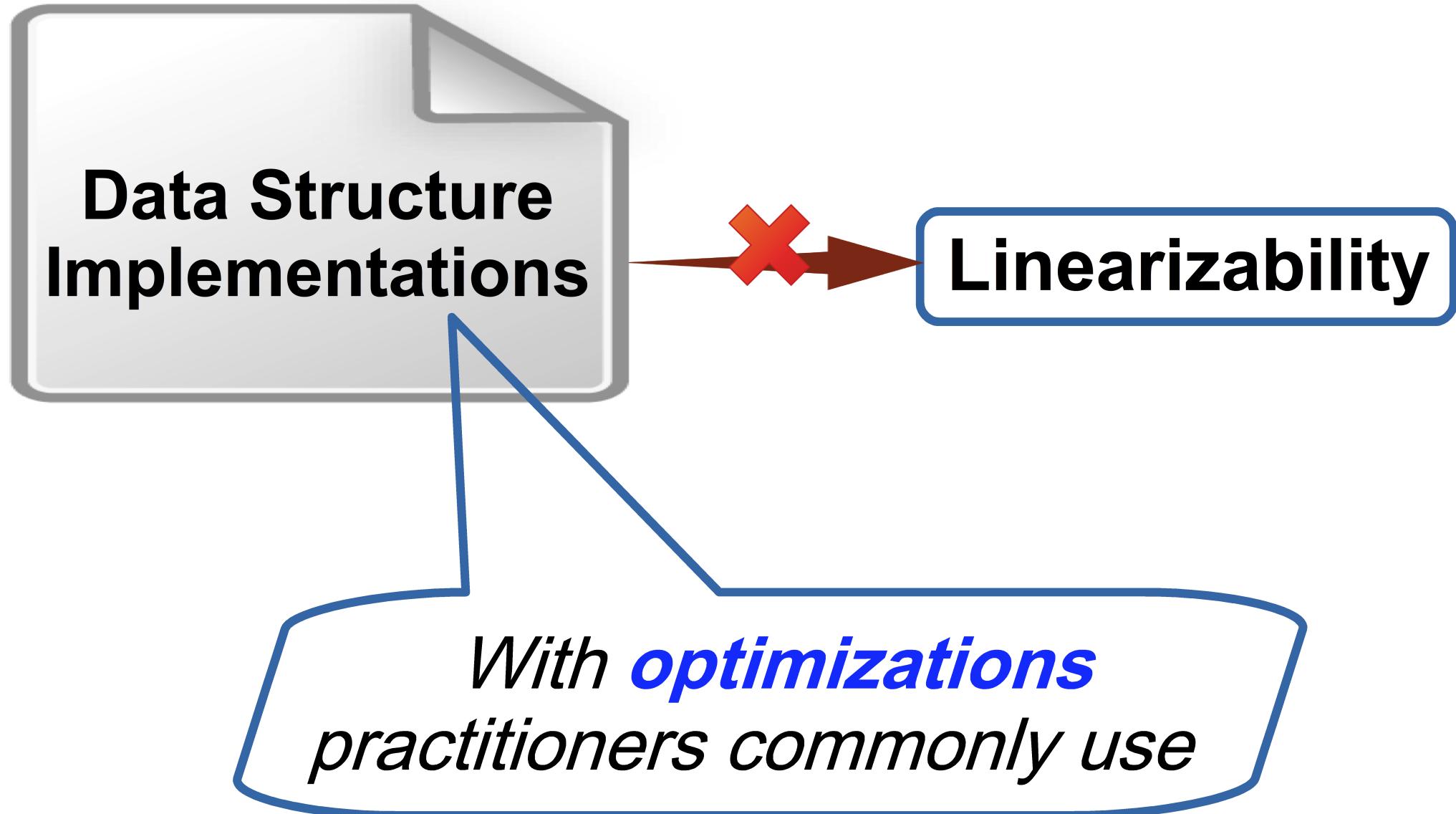
```
y.enq(2)  x.deq() → -1  x.enq(1)  y.deq() → 2
```

Linearizability Highlights

**Analogy to
sequential executions**

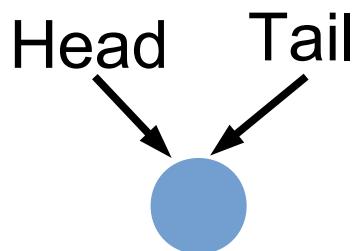
Composability

Optimizations Can Break Linearizability



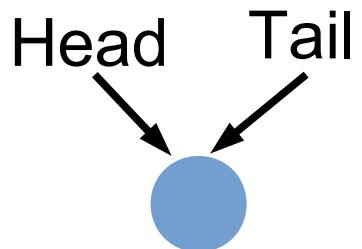
C++11 SPSC Queue Example

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struct Node {  
    atomic<Node*> next;  
    int data;  
};
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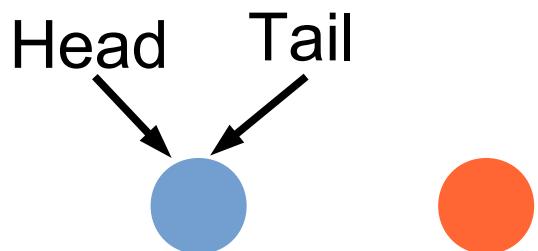
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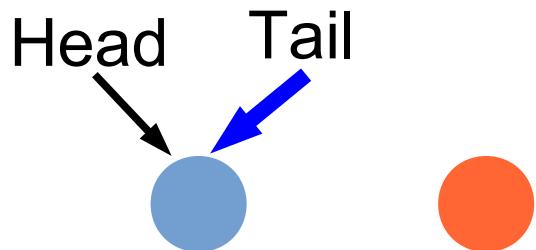
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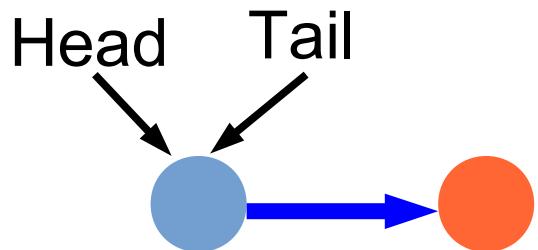
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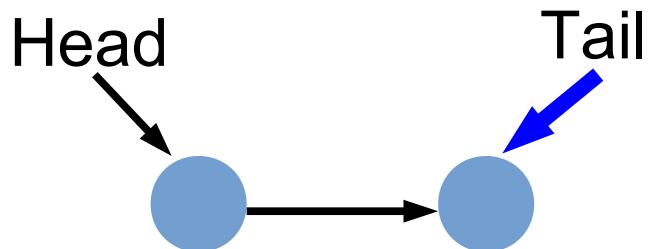
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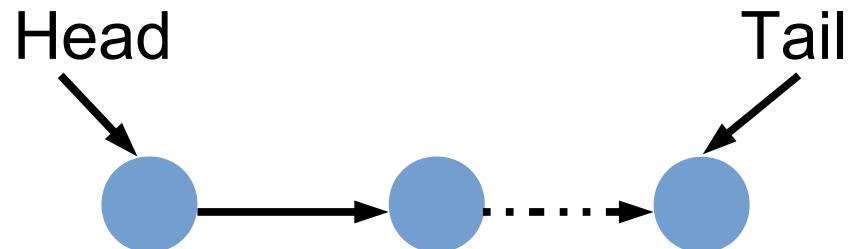
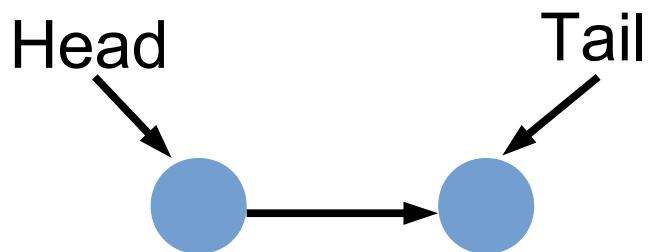
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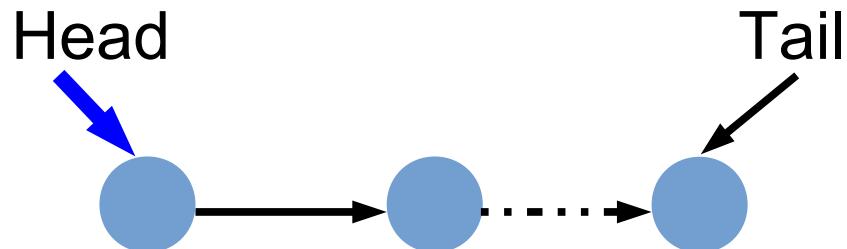
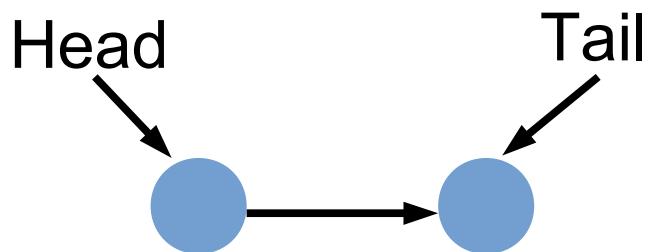


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int deq() {  
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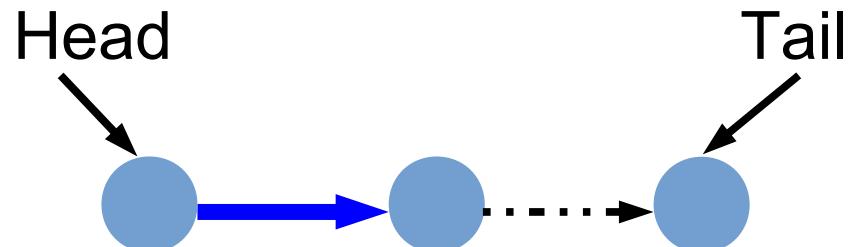
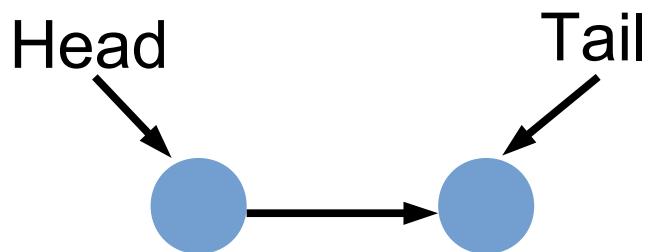


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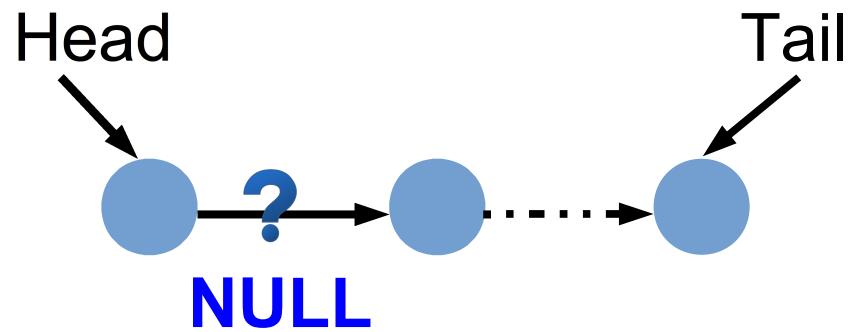
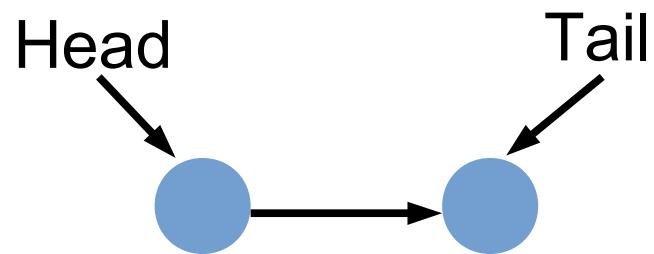


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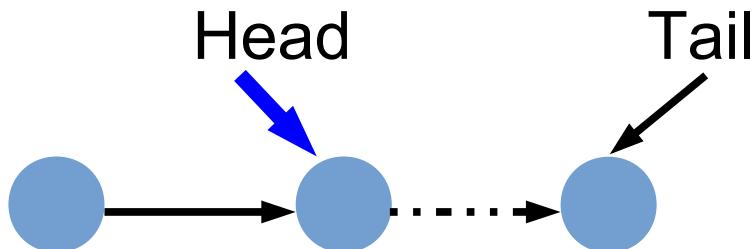
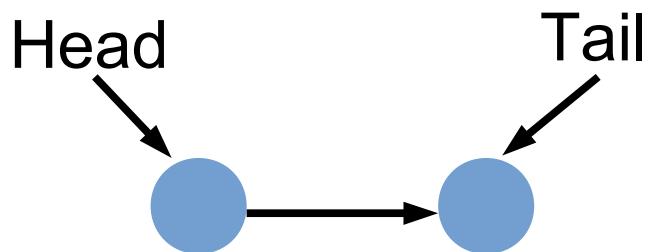


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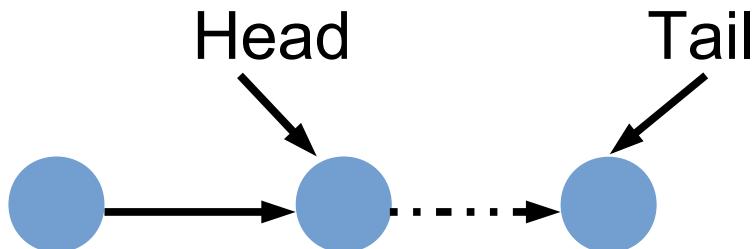
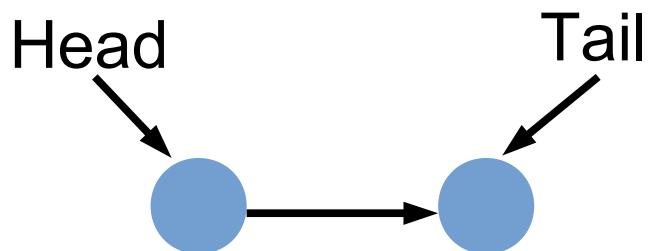


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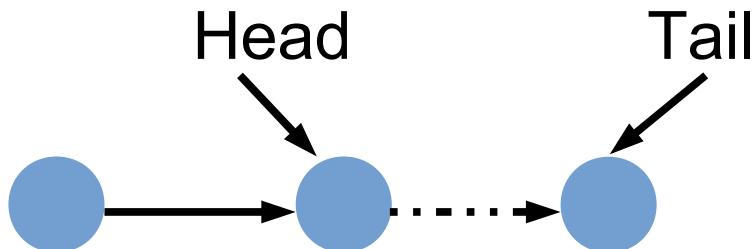
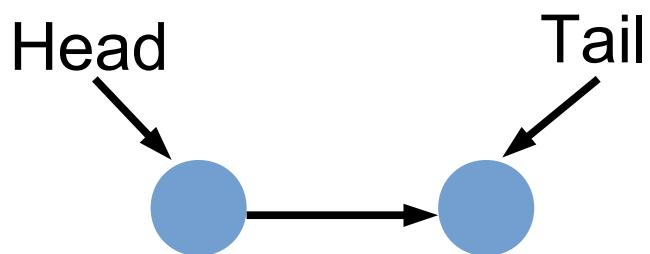


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```

Release-Acquire for Synchronization

```
// T1  
ptr = new Object();  
x.enq(ptr);  
synchronization → // T2  
r1 = x.deq();  
if (r1 != -1)  
    r2 = r1->field;
```

Ensures reading a
fully initialized object

Non-linearizable SPSC Execution

```
SPSCQueue x, y; // Initially empty  
// Thread 1           // Thread 2  
x.enq(1);           y.enq(2);  
r1=y.deq(); // → -1   r2=x.deq(); // → -1
```

Non-linearizable SPSC Execution

```
SPSCQueue x, y; // Initially empty
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```
// Thread 1
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```
x.enq(1);
```

```
r1=y.deq(); // → -1
```

```
// Thread 2
```

```
y.enq(2);
```

```
r2=x.deq(); // → -1
```



Both return empty (-1)

Non-linearizable SPSC Execution

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```
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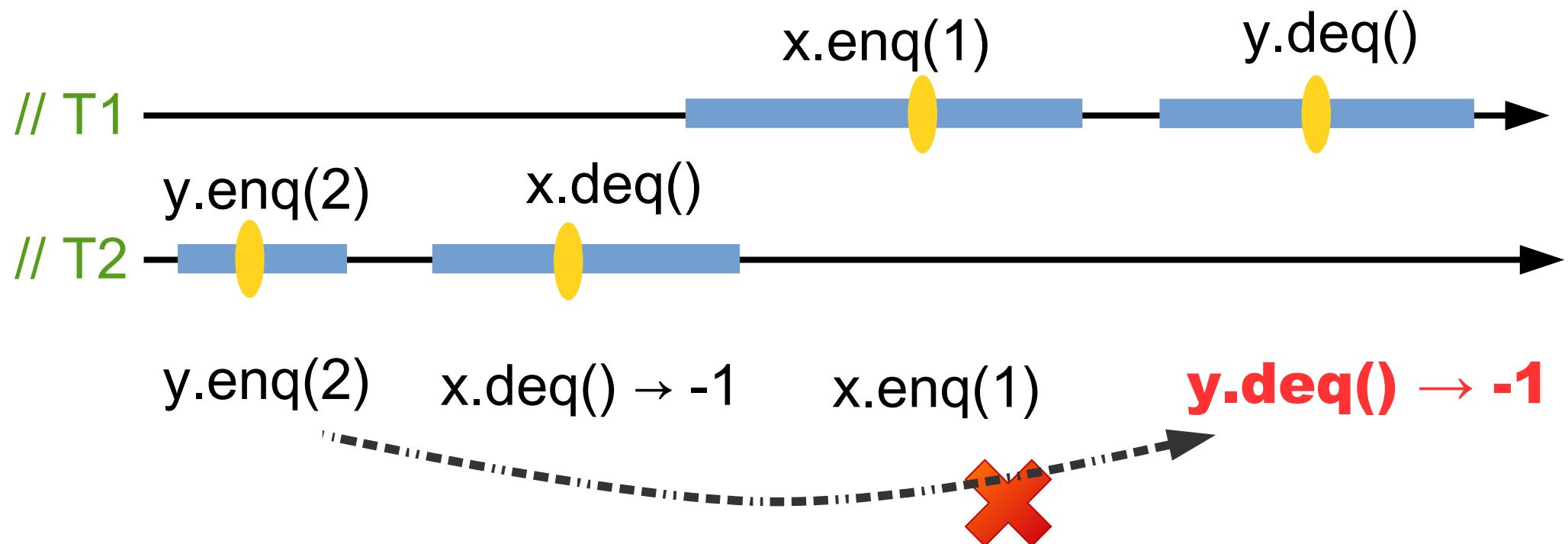
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Non-linearizable SPSC Execution

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// Thread 1 // Thread 2  
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r1=y.deq(); // → -1 r2=x.deq(); // → -1
```

Under the hood:

```
// Thread 1 // Thread 2  
next1.store(n1, release); next2.store(n2, release);  
...  
next2->load(acquire); //0 next1->load(acquire); //0  
return -1; return -1;
```

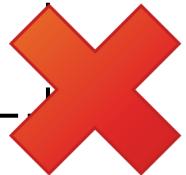
Alternative 1: Use the “seq_cst” ordering

```
SPSCQueue x, y; // Initially empty  
  
// Thread 1           // Thread 2  
x.enq(1);  
r1=y.deq(); // → -1  y.enq(2);  
r2=x.deq(); // → -1
```

Only SC executions (in absence of data races)

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```
SPSCQueue x, y; // Initially empty  
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Only SC executions (in absence of data races)

→ Problematic execution not allowed

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Only SC executions (in absence of data races)

→ Problematic execution not allowed

→ Linearizability applies

→ **Performance loss**

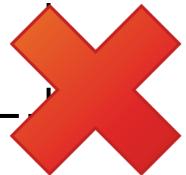
Alternative 2: Constrain Usage Patterns

```
SPSCQueue x, y; // Initially empty  
  
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enq() and deq() on the same queue must conflict with each other

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```

enq() and deq() on the same queue must conflict with each other

- Problematic execution not allowed
- Linearizability applies
- **Limited usefulness**

Alternative 3: Weaken the Specification

```
SPSCQueue x, y; // Initially empty  
// Thread 1           // Thread 2  
x.enq(1);           y.enq(2);  
r1=y.deq(); // → -1   r2=x.deq(); // → -1
```

deq() of the sequential FIFO can spuriously return empty (-1)

Alternative 3: Weaken the Specification

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SPSCQueue x, y; // Initially empty
```

```
// Thread 1
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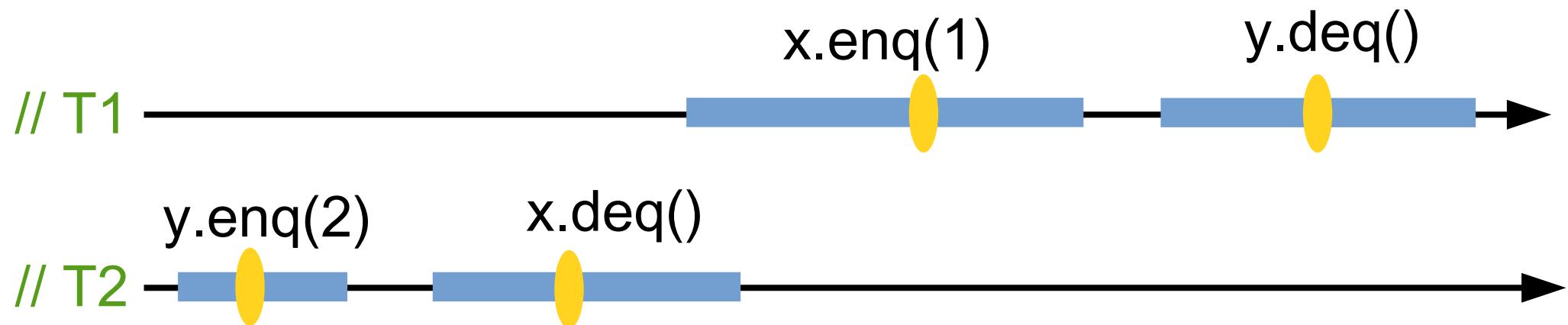
```
x.enq(1);
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```
r1=y.deq(); // → -1
```

```
// Thread 2
```

```
y.enq(2);
```

```
r2=x.deq(); // → -1
```



`y.enq(2)` `x.deq() → -1`

`x.enq(1)`

`y.deq() → -1`

Trade-off between Alternatives

	Use strong ordering	Constrain Usage	Weakened Specification
Performance	✗	✓	✓
Usefulness	✓	✗	✓
Clean Semantics	✓	✓	✗

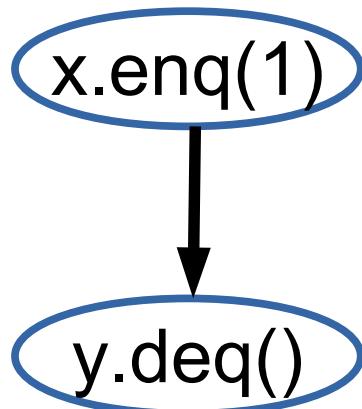
Our Correctness Model

- **Admissibility**
 - Explicit condition under which the data structure's semantics is well defined

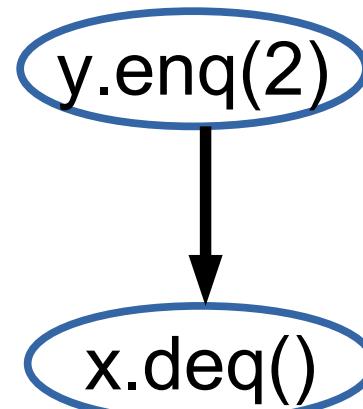
Admissibility – Option 1

enq() and deq() are not required to conflict with each other

// Thread 1



// Thread 2

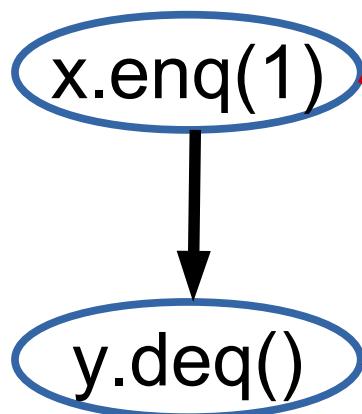


Non-deterministic FIFO

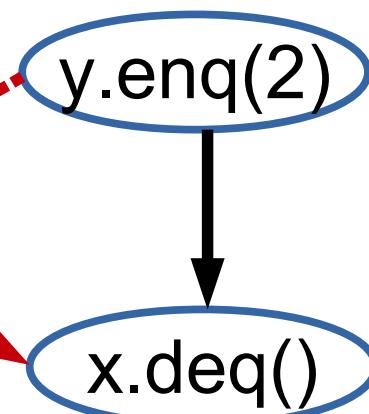
Admissibility – Option 2

enq() and deq() must conflict with each other

// Thread 1



// Thread 2



Deterministic FIFO

Our Correctness Model

- **Non-deterministic specification**
 - Concurrent execution → equivalent sequential execution
 - Non-deterministic equivalent sequential data structure

Our Correctness Model

- **Non-deterministic specification**
 - Concurrent execution → equivalent sequential execution
 - Non-deterministic equivalent sequential data structure



A sequential FIFO, whose `deq()` operation can spuriously return -1

Problem: Too Weak Specification

```
// Same thread  
x.enq(1);  
r1=x.deq(); // → Spuriously return -1
```

- **The spec can become too weak**
- Can go beyond developer's expectation

Solution: Tighten the Weakened Spec

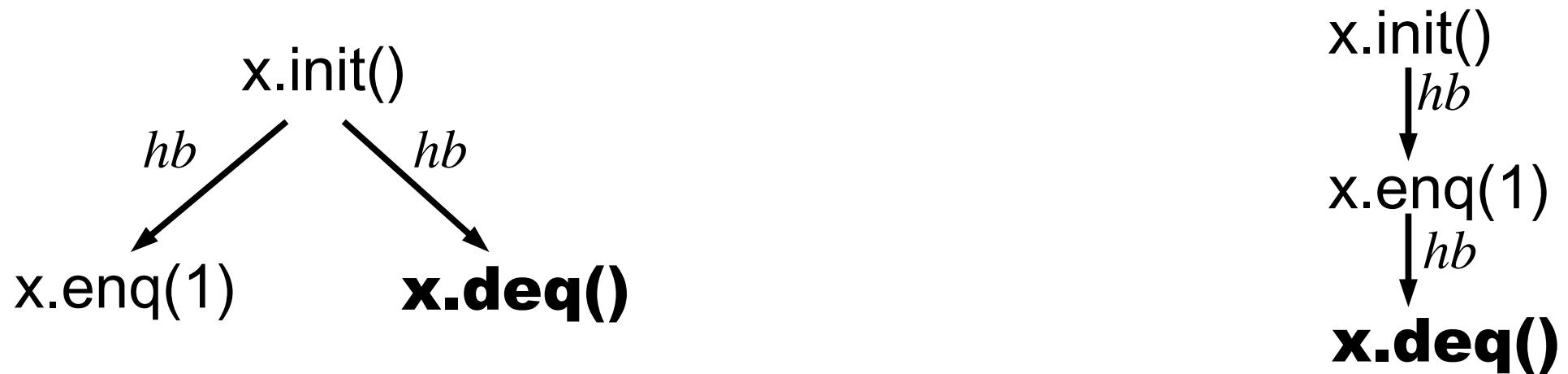
```
// Same thread  
x.enq(1);  
r1=x.deq(); // → Spuriously return -1
```

Specify when deq() can spuriously return empty (-1)!!

Tighten Spec with Justifying Prefix

Justifying prefix

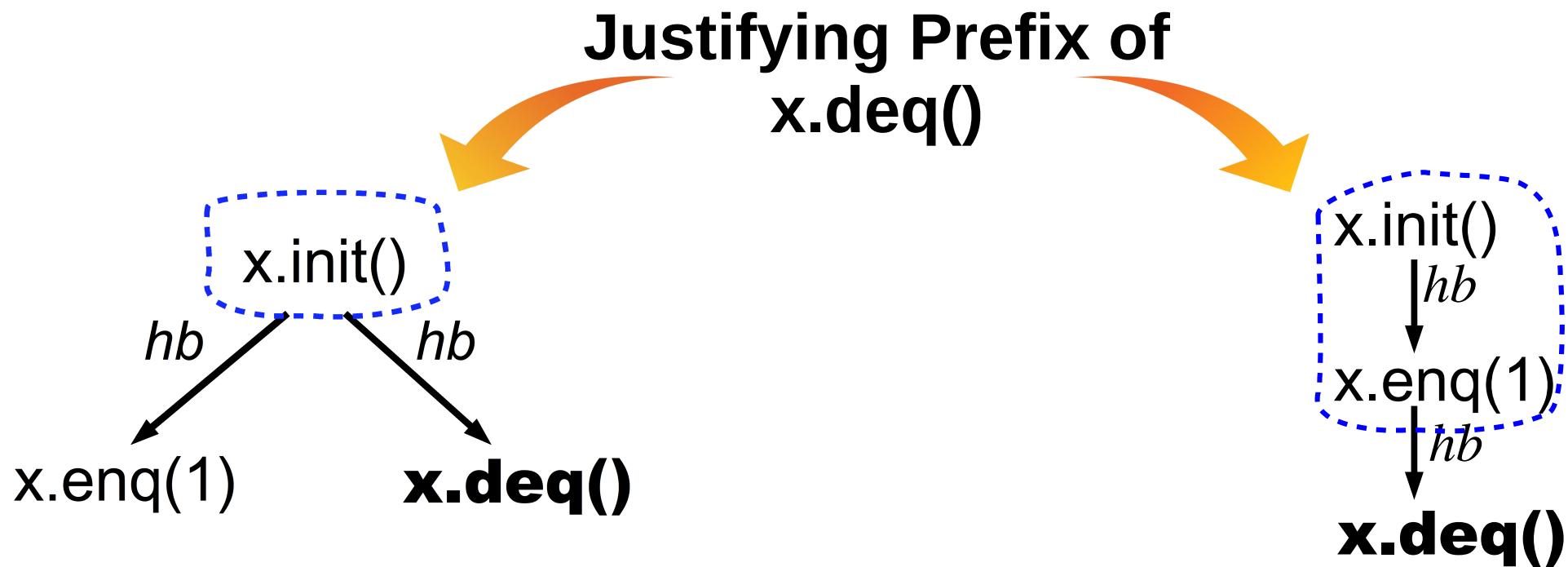
→ sequence of method calls that are ordered by *happens-before* and that *happen before* a method call m



Tighten Spec with Justifying Prefix

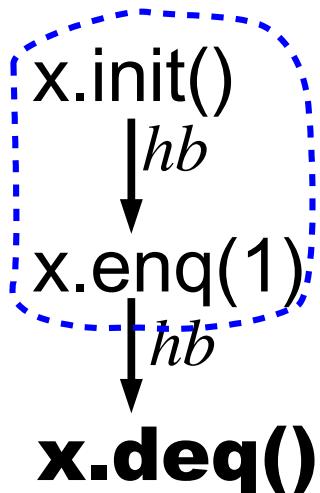
Justifying prefix

→ sequence of method calls that are ordered by *happens-before* and that *happen before* a method call m



Tighten Spec with Justifying Prefix

deq() spuriously return -1 **only when** one of its justifying prefix empties the queue



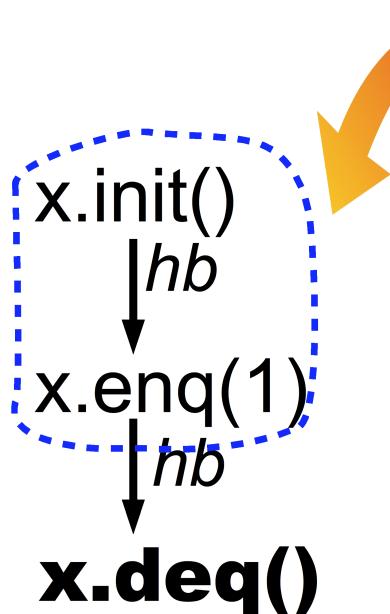
// Same thread

```
x.enq(1);  
r1=x.deq(); // → Return -1
```

Tighten Spec with Justifying Prefix

deq() spuriously return -1 **only when** one of its justifying prefix empties the queue

Justifying prefix enqueues 1 to the queue



```
// Same thread  
x.enq(1);  
r1=x.deq(); // → Return -1
```



Non-deterministic Linearizability

- Admissibility
- Non-deterministic specification
- **Constrain non-determinism with justifying prefix**

Composability!

CDSSPEC Specification Language

- A concurrent data structure specification language
 - Based on non-deterministic linearizability

Admissibility

```
/** @Admit: deq <-> deq (true);
@Admit: enq <-> enq (true) */
```

```
void enq(int val) {
    Node *n = new Node(val);
    Node *t = Tail.load(relaxed);
    t->next.store(n, release);
    Tail.store(n, relaxed);
}
```

Equivalent Sequential Data Structure

```
/** @DeclareState: IntList *q; */
```

```
void enq(int val) {  
    Node *n = new Node(val);  
    Node *t = Tail.load(relaxed);  
    t->next.store(n, release);  
    Tail.store(n, relaxed);  
}
```

Ordering Points to Order Method Calls

```
/** @DeclareState: IntList *q; */
```

```
/** ... */  
int deq() {  
    Node *h = Head.load(relaxed),  
        *n = h->next.load(acquire);  
    /** @OPDefine: true */  
    if (!n) return -1;  
    Head.store(n, relaxed);  
    return h->data;  
}
```

Dequeue – Side Effect

```
/** @DeclareState: IntList *q; */
```

```
/* @SideEffect: if (C_RET== -1) return;  
S_RET = STATE(q)->pop_front();
```

```
*/
```

```
int deq() {  
    Node *h = Head.load(relaxed),  
        *n = h->next.load(acquire);  
    if (!n) return -1;  
    Head.store(n, relaxed);  
    return h->data;  
}
```

Dequeue – Postcondition

```
/** @DeclareState: IntList *q; */  
  
/** ...  
 * @PostCondition: return C_RET== -1 || C_RET==S_RET;  
 */  
int deq() {  
    Node *h = Head.load(relaxed),  
        *n = h->next.load(acquire);  
    if (!n) return -1;  
    Head.store(n, relaxed);  
    return h->data;  
}
```

CDSSPEC Checker

- **Back-end analysis** of the CDSChecker model checker
 - Exhaustively check a given test case against CDSSPEC specifications (under some constraints)

Expressiveness of CDSSPEC

- **10 real-world data structures**
 - 3 concurrent queues: SPSC, M&S queue & MPMC
 - 4 locks: Linux RW lock, Seqlock, MCS lock & Ticket lock
 - A read-copy-update implementation
 - Chase-Lev deque
 - Concurrent hashtable

CDSSEPEC Checker Performance

- Ubuntu 14.04 (Intel Xeon E3-1246 v3)

Benchmarks	Total Time (sec)
Linux RW lock	13.71
MPMC queue	4.83
MCS lock	3.00
Ticket lock	0.17
Chase-Lev deque	0.10
M&S queue	0.03
SPSC queue	0.01
Seqlock	0.01
RCU	0.01
Concurrent hashtable	0.01

within 15 sec

9/10 within 5 sec

The table shows performance metrics for various benchmarks. The 'Linux RW lock' benchmark has a total time of 13.71 seconds, which is highlighted with a cyan background. The remaining nine benchmarks have total times ranging from 0.01 to 4.83 seconds. A blue curly brace groups the last nine benchmarks, and a blue arrow points from the text 'within 15 sec' to the 13.71 value. Another blue curly brace groups the first nine benchmarks, and the text '9/10 within 5 sec' points to the 0.17 value.

Finding Known Bugs

- Found 3 known bugs in 2 benchmarks
 - Weaker than necessary ordering parameters

Finding Injected Bugs

Benchmarks	# Injection	# Built-in	# CDSSpec
MPMC queue	8	0	4
Linux RW lock	8	0	8
MCS lock	8	4	4
Ticket lock	2	0	2
Chase-Lev deque	7	3	4
M&S Queue	10	3	7
SPSC queue	2	0	2
Seqlock	5	0	5
RCU	3	3	0
Hashtable	4	2	2
Total	57	15	38

Detected by
writing
specifications



Finding Injected Bugs

Benchmarks	# Injection	# Built-in	# CDSSpec	# Rate
MPMC queue	8	0	4	50%
Linux RW lock	8	0	8	100%
MCS lock	8	4	4	100%
Ticket lock	2	0	2	100%
Chase-Lev deque	7	3	4	100%
M&S Queue	10	3	7	100%
SPSC queue	2	0	2	100%
Seqlock	5	0	5	100%
RCU	3	3	0	100%
Hashtable	4	2	2	100%
Total	57	15	38	93%

100% for 9/10 benchmarks

Finding Injected Bugs

Benchmarks	# Injection	# Built-in	# CDSSpec	# Rate
MPMC queue	8	0	4	50%
Linux RW lock	8	0	8	100%
MCS lock	8	4	4	100%
Ticket lock	2	0	2	100%
Chase-Lev deque	7	3	4	100%
M&S Queue	10	3	7	100%
SPSC queue	2	0	2	100%
Seqlock	5	0	5	100%
RCU	3	3	0	100%
Hashtable	4	2	2	100%
Total	57	15	38	93%



>100,000
threads & a
16-bit counter
rollover

Ease of Use

- On average:
 - 11.5 lines per data structure
 - 1.22 lines per API method for ordering points

Related Work

- **Concurrent data structure specifications**
 - Refinement mapping, Commit atomicity, Concurrit, NDetermin
 - Relaxed memory model: Batty *et al.*, Tassarotti *et al.*
 - Bounded relaxation
- **Approaches based on linearizability**
 - Linearizability, Lineup, Paraglider, VYRD,
 - Techniques to automatically prove linearizability
 - Others: Concurrency-aware objects, list-based set
- **Enforce code to only admit SC behaviors**
 - Under TSO & PSO (Burckhardt *et al.*, Burnim *et al.*)
 - For C/C++11: Meshman *et al.*, AutoMO
 - Dfence (infer fences for hardware memory model)
- **Others:** GAMBIT, RELAXED, CheckFence

Conclusion

- **CDSSPEC**

A specification checker that allows developers to specify and check a range of concurrent data structures written with C/C++11

Questions

Questions??

Enqueue – Side Effect

```
/** @DeclareState: IntList *q; */  
/** @SideEffect: STATE(q)->push_back(val); */  
  
void enq(int val) {  
  
    Node *n = new Node(val);  
    Node *t = Tail.load(relaxed);  
    t->next.store(n, release);  
    Tail.store(n, relaxed);  
}
```

Ordering Points to Order Method Calls

```
/** @DeclareState: IntList *q; */
```

```
/** ... */
```

```
void enq(int val) {  
  
    Node *n = new Node(val);  
    Node *t = Tail.load(relaxed);  
    t->next.store(n, release);  
    /** @OPDefine: true */  
    Tail.store(n, relaxed);  
}
```

Dequeue – Justifying Postcondition

```
/** @DeclareState: IntList *q; */
```

```
/** ...;
@JustifyingPostcondition: if (C_RET== -1) return S_RET == -1;
*/
int deq() {
    Node *h = Head.load(relaxed),
        *n = h->next.load(acquire);
    if (!n) return -1;
    Head.store(n, relaxed);
    return h->data;
}
```